CONJUGATION AND HYPERCONJUGATION: A SURVEY WITH EMPHASIS ON ISOVALENT HYPERCONJUGATION

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Abstract-Various aspects and examples of conjugation and hyperconjugation are surveyed, and the **desirahtlity of an explicit classifation of both conjugation and hyperconjugation into two major** types, isovalent and sacrificial (ordinary) is emphasized. The existence of a third type, pluvalent conjugation, is also mentioned. Further, the desirability of a subclassification of isoconjugation and **isohypcrconjugation each into three sub-types (danve. non-dative. and homodativc. in orderof** increasing conjugative stabilization) is pointed out, with examples. Sacrificial conjugation and hyperconjugation are usually non-dative, but some examples of dative conjugation and hyperconjugation are cited. The intrinsic jointness of the inductive and mesomeric effects (both of which are forms of resonance) in homodative isoconjugation and isohyperconjugation is emphasized. Homodative alkyl isohyperconjugation in carbonium ions is discussed extensively, with especial reference to McCaulay's Conference paper. Some hitherto incompletely published theoretical evidence, supported by experimental spectroscopic evidence, that the ethylene positive ion is partially twisted in its ground state, is presented; the twist is due to incipient isohyperconjugation.

Definitions of the term hyperconjugation are considered with some care. It is suggested that the **Baker-Nathan effect (in so far as it refers IO differences bctwccn C-H and C-C hypcrconjugation)** should not itself be described as hyperconjugation, but rather as *differential* hyperconjugation. It is pointed out that there are no obvious theoretical reasons for expecting radical differences in stabiliza**tion cnqy or in magnitude of electron rclcasc between C C and C-H hypcrconjugation. Finally,** the writer wishes to apologize if he has sometimes gone astray in this paper because of the superficiality of his acquaintance with the vast literature of organic chemistry.

1. INTKODUCTION

(a) *General remarks*

MULLER and the writer in a recent paper' have shown by modified Hiickel-type LCAO-MO (LCAO molecular orbital) calculations how the observed relatively large stabilization energies in alkyl radicals and ions (relative to $CH₂$ and $CH₃$) can be understood in terms of hyperconjugative π -electron resonance. In seeking to understand the large size of the effects, they found it very illuminating to introduce a classification of hyperconjugativc (and of conjugative) effects in terms of types of major VB (valence-bond) resonance structures. Although these structures are in general very familiar,² it was felt that a systematic classification and terminology would be of real value.

Although corresponding LCAO and VB structures arc only roughly equivalent, the equivalcncc is probably usually good enough to form the basis for a qualitative classification which should be significant for both. Although the LCAO method is more useful for quantitative calculations, one can much more easily obtain fairly

¹ N. Muller and R. S. Mul1tkcn.J. *Amrr.* **Chem. Sue. 80. 3489 (19S8).**

⁹ G. W. Wheland, *Resonance in Organic Chemistry*. Wiley, New York (1955).

reliable qualitative³ insight into the reasons for the magnitudes of π -electron resonance effects in various kinds of cases by writing corresponding VB resonance strutturcs. (But see Section III(a), Notes added 20 November 1958).

The present paper contains a further development of the classification of conjugated and hyperconjugated molecules in terms of VB resonance structures, with examples. Since this paper was prepared in final form *ufler rhe Conference,* advantage has been taken of the opportunity to include in the discussion of examples commcntaries⁴ on some of the papers presented by others at the Conference.

In view of Dewar's strong advocacy at the Conference of the idea that the effects of π -electron resonance in ordinary conjugation, hence all the more so in ordinary hyperconjugation. arc inconsequential, one might bc persuaded that any further use of the idea of hyperconjugation has become **superfluous.** However, as is set forth in a separate complementary paper $*$ the writer is very doubtful that such an extreme viewpoint can be justified. Moreover, a major point in the present paper is that iso**valcnt** hyperconjugation should be a much stronger effect than ordinary hyperconjugation, because of resonance akin lo that in benzene. On the whole, it seemed best not lo consider the impact of Dewar's new ideas in the present paper, except incidentally. Resulting doubts and reasonable modifications of usual ideas will be examined **more carefully** in the separate paper mentioned.

(b) *Definitions of conjugation and hyperconjugarion*

A variety of phenomena in unsaturated and aromatic organic molecules, including those historically referred to as conjugation, have been explained in quantummechanical VB theory in terms of π -electron resonance between two or more classical VB structures. The use of the term conjugation has in recent years been increasingly extended to include all molecules believed to be stabilized by π -electron resonance; for example to benzene with its two equivalent Kekulé structures and to aniline with its quinoid in addition to Kekulé structures. In the present paper the word conjugation **will be** used in this broadened sense. *Conjugation* is then said lo exist in a molecule when the principal classical structure or structures contain single bonds each interposed between two multiple bonds or having on one side a multiple bond and on the other a lone π electron, π -electron pair or quartet, or π -electron vacancy. (For con**jugation** in the cumulcncs- see Section III(a)-a slight extension of this definition is needed.)

Hyperconjugated molecules can bc defined similarly if we regard a pair or triplet

 \mathbf{r} of bonds from an atom e.g. $\left(\sum_{R'} C$ or $\sum_{R'} C \right)$ as a quasi-double or quasi-trip Ð

bond
$$
\begin{pmatrix} R' \\ R \end{pmatrix} = C
$$
 or $\begin{pmatrix} R' \\ R' \end{pmatrix} \equiv C$. *First-order hyperconjugation* can be said to exist when the

^{*} R. S. Mulliken, Tetrahedron (1959) in press.

¹ IIowe~cr. quanllrarlve factors. which arc auromarically taken into account in rhc LCAO-MO method (though not very accurately unless retined forms of the method are used), can sometimes become so important as to seriously modify or even outweigh conclusions based on qualitative **Insight from VB structures.**

Thus the present paper incorporates (a) material prepared before the Conference: (b) responses to ideas and material presented by others at the Conference; (c) some improvements, refinements, and modifications resulting from the stimulus of the Conference papers and discussions. Finally (d) some additional comments believed important were inserted on 20 November 1958.

principal classical structure or structures contain single bonds interposed between one quasi-multiple bond and either an ordinary multiple bond, a lone π electron, π electron pair or quartet, or π -electron vacancy (with a slightly extended definition for cumulenes-see Section III(a)]. *Second-order hyperconjugurion* involves single bonds interposed between two quasi-multiple bonds; recent calculations⁶ indicate that the effects of second-order hyperconjugation should be quite small.

In the discussion of unsaturated or aromatic molecules with a planar skeleton of the unsaturated and directly attached atoms, the x direction will always be taken in this paper to be perpendicular to the skeletal plane. Then in any quasi-double bond, one is a quasi- σ and one a quasi- π , or quasi- π . Hereafter these will be designated as [σ] and $\lceil \pi_r \rceil$ or $\lceil \pi_r \rceil$ bonds.

For a group $H_2 =$ or $R_2 =$ (as for example in $H_2 = CO$ or $R_3 = CO$), let the bond orbitals of the two H atoms or of those R atoms which form the quasi-double bond be called a and b. Then the [o] GO (group orbital) has the form $a + b$, the $\lceil n_x \rceil$ or $[\pi_{\alpha}]$ orbital the form $a - b$ (omitting a normalizing factor in each case).

Fю. 1.

For a group $H_3 \equiv$ or $R_3 \equiv$, letting the three H_3 or R_3 bond orbitals of the quasitriple bond be called a, b, c, the [v] GO has the form $a + b + c$, while the $[\pi_x]$ and $\lceil n_{\nu} \rceil$ GOs are of the forms $a - b$ and $c - \frac{1}{2}(a + b)$, or vice versa (omitting normalization factors and neglecting overlap effects) or suitable orthogonal linear combinations of these, depending on how the triangle *ubc (see* Fig. I) is oriented with respect to rotation around the $R_3 \equiv$ bond. However, the hyperconjugative action is independent of the angle of such rotation. (This is no longer quite true for composite group:

 R' _k R' _R $\left\{\mathbb{R}\right\}$ = or $\left\{\mathbb{R}'\right\}$ =, insofar as the different R's are unlike in their hyperconjugative 1 R"

effectiveness.)

II. ISOVALENT CONJUGATION AND ISOVALENT HYPERCONJUGATION

(a) General characteristics; subclasses; interrelations of inductive and mesomeric *eflects*

In *isovalent conjugation* (or *isoconjugation* if one wants a briefer term) there are two or more classical structures containing equal numbers of π bonds, also of σ and of total bonds. The writer feels that it is worth while, and important,⁴ to distinguish

^{\bullet} Of course everyone knows these types, and perhaps most chemists will think it silly or presumptuous

L *C. A. Coulson* **and V. Crawford, J.** *Chcm. Sot. 2052 (1953);* **A. Lofthus.** *J. Amer. Chrm. Ser. 79. 24 (1957).*

^{&#}x27; IO give them names. but the writer is convinced that their overt recognition should make II easier to **think clearly about them.**

three main sub-classes of isovalent conjugation, namely (listing them in order of increasing expected resonance energy), (1) , dative, (2) , non-dative, and (3) , homodative. Typical examples are the following: (1) for the dative subclass, chlorethylene: isovalent dative structure H₂C -CH =CI⁻ in addition to main structure H₂C CHCI; or chloracctylcnc; (21, for the non-dative subclass, benzene and the ally1 radical: two equivalent isovalent structures each; (3) , for the homodative subclass, allyl ion or amidinium ion, or their derivatives: two equivalent isovalent structures each, with stabilization not only by resonance per se but also by *necessarily concomitant*⁷ partial uniformization of π charge distribution, brought about by the dative action involved in a shift from one of the two isovalent resonance structures to the other (e.g. $H_2C =$ CH: CH₂ to H₂C = CH - C⁺H₂). Two familiar further examples of dative isoconjugation (here superposed on benzenoid isoconjugation) are chlorobenzene and aniline. with dative isovalent structures C_8H_5 . \cdot Cl⁺ and C_8H_5 . N⁺H₂ respectively.

Dative isoconjugation involves exclusively one-way π dative action, which costs energy in creating an (often long) dipole, so that the dative structure, although isovalent with the main structure, is non-equivalent. On the other hand, homodative isoconjugation releases electrostatic energy by charge redistribution (equalization) as an *intrinsic part* of the total energy release by isovalent π -electron resonance. The resulting **bond** and charge distribution in the ally1 **ion may be summarized** by H_2C^+ i in CH in C^+H_2 .

But also, in the presence of either dative or homodative isoconjugation, *additional* "inductive" shifts of charge via both σ and π bonds must of course occur. In the dative case, they serve to lower the cncrgy of the dative resonance structure very conslderably and thus increase its importance for the molecule; for example in $CH₂CHCl$, Н,

 \overrightarrow{H} + CH \rightarrow Cl⁻ would much better describe the dative structure than H₂C \rightarrow H^2 σ

CH :CI-; then **in** the actual molecule, **when both the isovalent** resonance structures have been included, the Cl atom has lost π charge but gained σ charge.

In the homodative case, inductive effects serve to distribute some σ and also some π -electron positive charge to *all* the atoms in the molecule; the resulting distribution

might be described by $\frac{H}{H}$ C⁺¹ $\frac{\pi}{\sigma}$ CH $\frac{\pi}{\sigma}$ C+¹ $\frac{\pi}{\sigma}$ A major part of the π -

electron "inductive" redistribution, as compared with a single VB resonance structure, had, however, already been accomplished by isovalent resonance. Further, it should be especially noted that LCAO-MO π -electron calculations, in contrast to the usual VB formulations, automatically take into account *all* "inductive" as well as mesomeric n-electron charge shifts if allowance is made in the calculations for the effect of **its** charge on the π -electronegativity of each carbon atom.

In isovalent *hyperconjugation* (or isohyperconjugation), as in isoconjugation, there are in VB theory two or more rcsonancc structures containing equal Ioral numbers of bonds, and also containing equal numbers of σ and π bonds if one counts [σ] and $\lceil \pi \rceil$ bonds as σ and π bonds. Further, three main sub-classes of isohyperconjugation can usefully be distinguished, namely, (1). dative, (2) non-dative. and (3)

⁷ L. Goodman and H. Shull, *J. Chem. Phys.* 23, 33 (1955). For discussion of the corresponding **phenomena in** *hyperconjugation*, see references 1 and 11.

homodative; the characteristics of these classes parallel those of the corresponding **sub-classes** of isoconjugation.

lsohypexconjugation differs from isoconjugation in that there arc two (or in general **two sets** of) isovalcnt structures which differ (and hence are always non-equivalent) in a certain **special** way. Namely, the subordinate isovalcnt structures have one *more ordinary* π *bond and one less* [π] *bond* than the predominant structures; that it is the former **which are** subordinate is indicated by experimental evidence and justified by the belief that $[\pi]$ bonds are very considerably stronger than ordinary π bonds.

(b) *Datice isohyperconjugafion (and some new norarion)*

Let us first consider some examples from the dative sub-class, beginning with CH₃OH. The two isovalent structures are H₃ \neq C-OH and H₃⁻ \neq C \neq O⁺H The symbol \rightarrow represents a π_x bond and the symbol \rightarrow represents a π_y bond.¹ This or equivalent symbolism is useful in keeping track of π_x and π_y bonds when both types arc prcscnt, as is very frequently the case when one considers isovalent resonance structures in hypcrconjugation.

Even in conjugation, such symbolism is useful for a clear understanding whenever triple bonds, or cumulated bonds, are present: for example HC \equiv CCI, with two dative isovalent resonance structures HC $=C\neq$ Cl., HC \neq C \neq Cl. of equal importance, and a third less important one; allene with the single structure $H_2C=C\#CH_2$, or in more detail, $H_2 \# C \# C \# C \#H_2$; phenylacetylene with main structures like \mathscr{A} C \Leftarrow CH. This symbolism can of course be omitted whenever it is more trouble than it is worth.

Dative isohyperconjugation should occur in $(CH₃)₂O$ in a way similar to that in $CH_3OH: (H_3 \equiv C-\frac{1}{2}\bullet H_3$ $C=O\bullet Mc$, MeO $\bullet=C\bullet H_3$. CH₃NH₃, (CH₃)₂NH, and $(CH₃)₃N$ insofar as they may be treated as having a nearly planar arrangement of atoms bonded to the nitrogen present again a similar situation. Dative isohyperconjugation is again expected in CH₃Cl, the main structure being H₃ \equiv C-Cl, the main subordinate structures $H_3^- \rightleftarrows C \rightleftarrows C!$ and $H_3 \rightleftarrows C \rightleftarrows C!$. Dative isohyperconjugation here is closely analogous to dative isoconjugation in chloracetylcne. The foregoing examples illustrate how conjugation or hyperconjugation can bc either *one-dimensional* $(\pi_z \text{ only})$, or *two-dimensional* (both π_z and π_y). Another interesting example is H₂CO, with isovalent structures $H_{\overrightarrow{r}}C=O$ and $H = C=O⁺$.

In the foregoing examples the effects of isohyperconjugation are doubtless small, first because they arc dative (and the clfccts even of dative *conjugation* are relatively modcratc), and second because they are hypcrconjugative. The writer sees no sufficient reason, however, to assume that they arc entirely negligible.

Another interesting example is that of $H₂O₃$, where on the basis of spectroscopic evidence⁸ the two H-O-O bonds are in planes nearly perpendicular to each other. It is easily shown that a planar structure, either *cis* or *trans.* offers no possibility of isovalent hyperconjugation; only ordinary hypcrconjugation is then possible. If steric repulsions between the two H atoms wcrc **a** determining factor, the planar *trans* form should be preferred. For a 90° twisted form, dative isohyperconjugation

H H can occur to its maximum possible extent. Besides the main structure, $1 / \sqrt{1 + \frac{1}{2}}$ O-O

' E. Flirota. J. *C'hmm. fhys.* **20. 136 (19%). and rdcrmes cited therein.**

dative isovalent structures, $O \pm O^+$ and | and $\mathbf{I}^+ \rightleftharpoons \mathbf{OH}^-$ can be written. If we neglect $\mathbf O$

the fact, whose effect here should be minor, **that** the HO0 angles are somewhat greater than 90°, the left-hand OH bond is formed by a π_x oxygen electron leaving a π_y (and an s) lone pair on the atom, while the right-hand OH bond is formed by a π_v oxygen electron leave a π_x lone pair on that atom. By dative action, either a π_x , or a π_y , O = 0 double bond can be formed, as indicated in the isovalcnt structures above. Unfortunately this example cannot be used as a proof of the decisive importance of isovalent hyperconjugation, since π -electron non-bonded repulsions also favor the twisted form.⁹ Further, the actual twisted form according to Hirota's analysis[®] is only 1.29 kcal more stable than the planar cis form (and 0.59 kcal more stable than the planar *trans* form).⁸ Another similar example is that of N_2H_4 , where again the stable configuration is a twisted one which again is favored both by non-bonded repulsions^{9,10} and by isovalent hyperconjugation. In contrast, the planar structure of $C_2H₄$ is strongly stabilized by π_z -electron bonding although the twisted form would be favored by isovalent hyperconjugation. In $C_2 H_4$ ⁺, the latter apparently becomes partially dominant, causing twist. (The cases of C_2H_4 and C_2H_4' ' will be discussed below.)

A final example of dative isovalent hypcrconjugation where the effects may bc larger is that of boron trimethyl. The main structure is $B(-C=H_a)_a$, and there arc three isovalent structures of the type $Me₂B\pm C\pi H₃$. The fact that BMe₃ does not dimerize like BH₂ suggests that it has special stability in itself, due to isovalent hyperconjugation, which is not possible in $BH₃$. One may of course argue that the CH₃ group cannot replace an H atom in the diborane bridge, but, (a), there is no thcorctical reason why it cannot and (b) in $Al₂Me₆$ with structure analogous to diborane, the methyl group does function as a bridging agent.¹⁰ To be sure, $Me₂BH₂BMe₂$ is known, suggestmg that H but not Me can function in a bridge bond; but the dimerization of Me₂BH might also be explained by the lesser amount of hyperconjugation possible here; and/or H may be a *better* bridging agent than Me. Theoretical computations on hyperconjugation in $BMe₃$, for example by the Hückel method using reasonable empirical parameters, and with due allowance for the presence of strong B^+ - $C^ \sigma$ bond polarities ("inductive effect"), would bc of much interest.

(c) A'on-dative isohyperconjugation

If jts geometry conforms approximately to its conventional formula, as seems probable, the ethyl radical is a typical example of non-dative isohyperconjugation.¹ The main structure is then $H_3 \neq C$ -CH₂, with an odd π_x electron on the CH₂ carbon. The hyperisovalent resonance structure is $H_3 \# C = CH_2$, with a quasi- π_x odd electron

H' on the H₃. (This is equivalent to H $-C=CH_3$, as the hyperconjugation resonance $H₂$

structure is often written, provided, of course, suitable resonance among three such forms is understood.) The isopropyl and r-butyl radicals furnish similar examples,' Another example, ethylene twisted through 90°, will be discussed below. Alkylsubstituted triphenylmethyl radicals, on the other hand, furnish examples where

^l**W. G. Penney and G. B. B. M. Sulhcrland. J.** *Chrm. Phvs. 2.492 (1934).*

^{&#}x27;* **R. S. hlulliken.** *('hem. Rco. 41, 207 (1947).*

isohyperconjugation. though thcorctically cxpcctcd. is apparently unimportant, but for reasons which appear understandable (see footnote *33).*

(d) *Homodative isohyperconjugation*

The alkyl and the aromatic carbonium ions furnish numerous examples of homodative isohyperconjugation. In agreement with experimental evidence, the energy effects of isovalcnt hyperconjugation should be at a maximum in the homodative **sub. class.** LCAO-MO computations on the alkyl ions (assuming conventional geometry) have been presented by Muller and the writer.¹ Taking the ethyl cation as a typical example, the main structure is $H_3 \oplus C \rightarrow C^{\dagger} \oplus H_3$, the hyperisovalent resonance structure is H_3 ⁺ \star ;C \neq C H_2 . Arrowheads have been added to indicate inductive effects; for the π_x electrons, these are automatically included in the LCAO computations (cf. Section II (a) for a fuller discussion in the analogous case of homodative isoconjugation). In our paper, we also included π_x inductive effects because we allowed for $\pi_{\bf v}$ as well as $\pi_{\bf x}$ hyperconjugation. (Here $\pi_{\bf v}$ hyperconjugation is of the ordinary, not isovalent type.)

A related example would be that of the ethyl anion.

The carbonium ions derived from benzene and alkylatcd bcnzcnes by addition of a proton have been extensively studied by McCaulay and by Kilpatrick, and their collaborators. and those from polycyclic aromatic hydrocarbons by Mackor et *a/."* Semi-empirical LCAO computations on the simplest of these, the bcnzenium ion C_4H_7 ⁺, indicate that homodative isohyperconjugation between three ring-positive

isovalent structures of the type $\left\langle \right\rangle = H_2$ and two hyperisovalent Kekulé-type

structures \leq -H₂⁺ should strongly stabilize the ion.¹² Let us call this Kekulé hyperconjugation.

In all the mcthylated (or alkylated) benzene carbonium ions, the same type of isohyperconjugation should occur, $plus$ methyl (or alkyl) isohyperconjugation involving homodative transfer of π -electron positive charge to the methyl (or alkyl) groups.¹³ The simplest case is that of the toluenium ion. This should exist in six isomeric *forms*¹⁴ depending on which of ring atoms 1 to 6 accepts the proton. Let us consider the

4-tolucnium ion $(Me\ll \sqrt{2})^+$, with its three isovalent ring-positive structures such جاءِ as $H_3 \neq C \leq \sum H_3$ and two isovalent Kekule-hyperconjugation structures, just ic as in the benzenium ion, and *in addition* one isovalent methyl-hyperconjugation structure $H_3 = C \rightarrow L_1$. Isovalent methyl hyperconjugation is possible in toluenium ions for 2.4, or 6 addition of the proton; less stable isomers with the added

¹¹ E. L. Mackor, G. Dallinga, J. H. Kruizinga and A. Hofstra, *Rec. Trav. Chim. Pays-bas* 75, 836
186 (1956); F. L. Mackor, A. Hofstra and J. H. van der Waals, *Trans. Faraday Soc.* 54, 66, 186) (1958) ; and numerous other papers.

¹² N. Muller, L. W. Pickett and R. S. Mulliken, *J. Amer. Chem. Soc.* 76, 4770 (1954). Note that all n -electron inductive effects are automatically included (cf. discussion in Section II(b) of the analogous situation in homodative isoconjugation).

¹⁸ D. A. McCaulay and A. P. Lien, J. Amer. Chem. Soc. 73, 2013 (1951); D. A. McCaulay's, Tetra*h&on.* **This issue.**

I4 The word "isomeric" is not strictly appropriate here. since some of the formsare indistinguishabk. But its use. m this section. will be very helpful in making things clear.

proton in the 1, 3, or 5 position should exist but without methyl isohypcrconjugation, hence with stability about like the bcnzcnium ion. Attribution of the observed increasing base strengths of increasingly methylated bcnzcncs to methyl hyperconjugation, as proposed by McCaulay,¹³ by no means necessarily implies that this is more effective than Kekulé hyperconjugation. The latter (which is equally present¹⁵ in all the methylated benzenes, and for all six isomers of each) should be present as a more or less constant background factor in all, supplemented by methyl hyperconjugation to an extent which depends on the numbers and positions of the substituted methyl groups. Although the basicity of benzene is very low, it seems entirely likely that the Kckulé hyperconjugation may be of predominant importance in creating a *minimal* basicity in benzene which is then *enhanced* to notable levels of strength by successive increments of methyl hyperconjugation. Theoretical computations by the LCAO-MO method on methylated benzenes would be of great interest in this connection.

As already noted, each carbonium ion derived from benzene or any methylated benzcnc by protonation can exist in six isomcric forms. For *each* of these isomers, methyl isohyperconjugation with some definite number M of methyl groups, from zero to a maximum of three, can occur, as one can see by drawing VB structures and keeping only those which are isovalent with the ring-positive and Kekulé-hyperconjugated structurcs.'6 If isohypcrconjugativc stabilization is the main determining factor. the basicity of any mcthylatcd benzene should depend primarily on the *lurgesl M due* possessed by any *of Ihe isomers* of its carbonium ion, and should bc greater for larger maximum M ; isomers with less than the largest M for that particular molecule should count very little for its basicity, because of their lower stability. On the other hand, the basicity should be greater the greater the *number N* of isomers of *maximum M.*

Table 1 lists the numbers of isomers of each M type for each of the methylated bcnzcncs, and also gives the relative basicity as reported by McCaulay in his Conference paper. It will be seen that the various molecules fall into groups in which the basicity is indeed primarily governed by the maximum *M* which appears for any of its isomeric forms, and also increases somewhat with the N value for maximum M. The striking increases in basicity from p - and o -xylene to m-xylene and to mesitylene parallel an increasing maximum *M.*

Inspection of Table 1 shows that an additional factor also somewhat influences basicity. In parentheses following the number N of isomers for any M type for any carbonium ion, in Table 1, is a number (say n) which says how many of these isomers have the added proton attached to the same ring atom as a methyl group. It will be seen that basicity increases somewhat as n/N for the *maximum-M* isomers increases. For example, the mcsitylene, isodurcnc, and pcntamcthylbenzcne carbonium ions all have the same $N(3)$ for the same maximum $M(3)$ but with $n \to 0, 1$, and 2 respectively; and the basicity increases with n/N . The hexamethylbenzene carbonium ion has $N =$ 6 for its maximum M (again 3) but now $n/N = 1$ since the added proton is necessarily attached to a methyl-bearing ring carbon in *all* isomers. Both effects evidently

¹⁶ Additional hyperconjugated structures having one less valence bond *(ordinary hyperconjugation)* although left out of account here, may perhaps also have *some* influence in determining basicity.

¹⁵ Except that proton addition to methylated ring atoms (which should certainly occur) may be somewhat more (or less) effective than to non-methylated ring atoms: half-CC instead of all-CH hyper**conjugation.**

TABLE 1. NUMBERS N OF ISOMERS OF METHYLATED-BENZENE CARBOSIUM IONS BELONGING TO VARIOUS M TYPES (first four columns of numbers; see text for explanation of M).

Fach number N is followed by a second number n in parentheses which tells how many of the N isomers have the proton attached to a methyl-bearing ring carbon. The basicity (last four columns of numbers from McCaulay's Conference paper¹³) is seen to be determined essentially only by those isomers which have maximum M (indicated in the first four columns by bold face type).

increase the basicity. The enhancement of basicity associated with attachment of a proton to a methyl-bearing ring carbon may reasonably be explained as due to inductive stabilization of isomers of this type, consequent on release of some negative charge by the methyl carbon to the ring carbon to which it is attached.

Further minor factors somewhat influencing the basicity of aromatic carbonium ions perhaps include steric effects, ordinary hyperconjugation,¹⁶ the presence of isomers with less than maximum *M* values, diffcrcnces in solvation effects, and perhaps others.

It is of interest that Table 1 indicates that the basicity of toluenc, too small to bc accurately determined but estimated as 0.01 by McCaulay, should bc considerably larger (say about 0.3) to be consistent with the rest of Table 1.

(e) Isoh_sperconjugorion in 90"-twisted ethylene and in GH,+.

Ethylene with the two CH, planes twisted to perpendicularity ("perp. C_2H_a ") was perhaps the first recognized example of hyperconjugation, although the name was not then used. Later Roothaan and the writer made a scrics of LCAO-MO computations on ethylene in its ground state and three excited states, and on C_2H_4 ⁺, for angles of twist ϕ ranging from 0° (planar) to 90°.¹⁷ Semiempirical parameter values similar to those used in more recent computations⁵ were used, and the effect of π -electron overlap was included. Both π_r and π_s hyperconjugation were taken into account, as becomes obviously necessary as $\phi \rightarrow 90^{\circ}$. Our 1947 paper was intended to be preliminary, and failed to report certain details of our computations. Some of the results on C_1H_4 which arc of particular interest in the present connection will be reported below.

For planar C_2H_4 , the VB structure is $H_2C=CH_2$, or if one wishes to consider $\pi_{\mathbf{v}}$ hyperconjugation (which is second-order, and *not* isovalent), $H_{\mathbf{r}} = C \leftarrow H_{\mathbf{v}}$. For perp. C_2H_4 , the main VB structure $H_{\overline{277}}\dot{C}-C=\mathbf{H}_2$ is in resonance with the two

P. S. Mulliken and C. J. Roothaan, *Chem. Rev.* **41, 219 (1947). Note that the symbol δ is generally** used to mean what is here called δ/β .

isovalent hyperconjugated structures $H_f-\dot{C}$ $\neq C=\dot{H}_f$ (π_r hyperconjugation) and $H_2 \rightarrow C \rightarrow C^{-1}$, (π, h) hyperconjugation).

For planar C_2H_4 ⁺ the VB structure may be represented as $H_2 \pi r C^{+1} \rightarrow C^{+1} \pi r H_6$. For perp. $C_2H_4^+$, the electronic state would be ²E of symmetry D_{sd} , for which there are two independent though equivalent orbital wave functions (twofold orbital degeneracy). For *one* of these (in the other, the \cdot and $+$ would be interchanged), the main VB structure $H_2 \overrightarrow{H} - C_2 \pm H_2$ is in resonance with the homodatively isovalent hypercon-

FIG. 2. Theoretically computed orbital energies (in eV) of ground states of C_1H_4 (state N, below) and $C_{\sharp}H_{4}^*$ (state 1, above) as functions of angle of twist ϕ . From unpublished work of Mulliken and Roothan (cf. reference 18). Full line curves are for best parameter values used (β^* – 2 β , δ = 0, β – -3 eV; dot-dash curves are for the case of no *hyperconjugation;* dashed curves for $\beta^* = 1.5\beta$, $\delta = \beta$, $\beta = -3$ eV.

jugated structure $H_{\text{g}}-\text{C} \rightleftharpoons \text{C}-H_{\text{g}}$ and with the neutrally isovalent structure $H_1 \rightleftarrows C \rightleftarrows C-H_2$. (Note that these three structures correspond to those of perp. C_1H_4 if one replaces one \cdot by a $+$ in each.)

Fig. 2 shows the computed curves that we obtained for C_2H_4 and $C_2H_4^+$, but did not publish in 1947, for each of three choices of semiempirical parameters:¹⁷ (a) no hyperconjugation $(\beta^*) \gg \beta$; (b) $\beta^* = 1.5\beta$, $\delta = \beta$; (c) $\beta^* = 2\beta$, $\delta = 0$. Of these, the third choice is the most nearly correct according to recent views (β^*/β) measures the degree of reluctance of an H_2 to give up its quasi- π bond in favor of a C C bond, while δ measures the tendency of H₂ to release an electron to carbon; values of β^*/β of 2.0 and of δ about -0.3β to -0.5β , corresponding to electropositive behavior of the H_2 group, have been currently accepted.⁵) Our curve for case (c) shows about 20 kcal stabilization by isovalent hyperconjugation in case (c); with $\delta/\beta < 0$, this would be somewhat increased.

For $C_2H_4^*$, allowance should have been made, as in later papers,^{1, 12} for an additional parameter to take account of the increase in electronegativity of positively charged atoms, but it is probable that this and $\delta/\beta < 0$ would give for C_sH_a ⁺ an energy-angle curve of the same qualitative character as in case (c) but with intensified departure from cases (a) and (b). It will be noted that curves (a) and (b) have a flat minimum at $\phi = 0$ ^o corresponding to stability of planar $C_2H_4^+$, while case (c)-evidently as a result of incipient isovalent hyperconjugation-shows a low maximum at $\phi = 0^{\circ}$ and shallow minima at perhaps about $\phi = 30^{\circ}$; but still a fairly high barrier at $\phi = 90^{\circ}$. This partial twisting may be understood by considering the following pair of VB structures for planar C_2H_4 : $H_2-C=\mathbb{C} \overline{H}_1$ and $H_2\overline{H}_2C=\mathbb{C}-H_2$. As long as C_1H_4 ⁺ remains planar, these *cannot mix* with the main VB ground state structure given above, because they belong to excited states with wave functions sharply difIerent in symmetry from the latter. But if twisting occurs, the symmetry distinctions are relaxed, and they can begin to mix in. (It may be remarked that description and understanding are easier using LCAO-MO theory.)"

It is now of great interest that experimental vacuum-ultraviolet spectroscopic data 18 on Rydberg states of C_2H_4 and C_2D_4 (which are essentially states of the ethylene positive ion plus an electron in an orbital so large that it has scarcely any influence on the molecular geometry) show unusual features which seem to be impossible to reconcile with a planar structure for $C_zH₄$ ⁺, but which seem to be just about what might bc expected for an energy-angle curve like the computed one for case (c) in Fig. 2. While an alternative interpretation of the spectroscopic data, involving excitation of a low-frequency out-of-plane bending instead of twisting frequency in the upper state. cannot be excluded with certainty, it seems much less probable. However, it is planned to make further experimental studies as soon as feasible which it is hoped may settle this question definitely, since there seems to be here an important probable confirmation of predicted effects of hyperconjugation.

111. **SACRIFICIAL (ORDINARY) CONJUGATION AND HYPERCONJUGATION**

(a) *General discussion*

Ordinary conjugation and hypcrconjugation are *sacrificial.* in the sense that π -electron resonance stabilization is effected only by structures in which, as compared with the single dominant VB structure, one π bond has been lost. In the following discussion in this Section the qualifying adjective "ordinary" or "sacrificial" will usually be assumed to be understood when "conjugation" or "hypcrconjugation" is used.

In the familiar example of 1,3-butadiene, with the dominant structure $H_2C = CH CH = CH₂$, there are three minor structures which may collectively be symbolized by H₂C-CH = CH-CH₂. The two \circ here represent either two \cdot (odd electrons, between which there is a "long bond"), or $+$ and $-$, or and $+$ (two equivalent ionic structures of opposite polarity).

¹⁸ P. G. Wilkinson and R. S. Mulliken, J. Chem. Phys. 23, 1895 (1955); P. G. Wilkinson, Canad. **1. Phys. 34, 643 (1956).** Stretching of the molecule in the ionized state also occurs; the twisting effect is approximately independent of this according to the spectroscopic data. When these papers were written the present Fig. 2, buried in the files, had been forgotten. In the first of these papers,
an effort was made to explain the Rydberg spectra using a planar model with a very flat minimum for C₂H₄^{*}. However, as time went on, we felt more and more convinced that the data pointed to a **twisted model. Finally, only recently. the earlier calculated curves here reproduced as Fig. 2. were rediscovered.**

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Very likely (although this point seems usually not to be recognized) the two ionic structures are much less important than the long-bond structure, since much more energy would be needed 10 create them. One should also especially note that this pair of structures involves two-way π dative action, as contrasted with the one-way π dative action involved in the subordinate VB structures in dative isoconjugation.

(Note added 20 *November* 1958. Recent calculations on butadiene by Berry¹⁹ based on LCAO-MO wave functions throw light on this question. He finds that the

VB structures C- C-C \cdot C, \hat{C} -C \cdot C- \hat{C} , and $\dot{\bar{C}}$ - \hat{C} = \hat{C} - \hat{C} make up roughly 35, 5, and 0.6 per cent of the wave function, while simple ionic structures $C = C^2 - C^2$ and C^{\pm} -C:=C make up 29 per cent and dispersion-type structures²⁰ C:-C--C:-Cand C^{\dagger} -C⁺-C⁺-C⁺ 30 per cent. These figures substantiate the unimportance of C^{\perp} -C- C^{\perp} , but indicate that other ionic structures may be more important even than $C-C' = C-C$ in contributing to the π -electron resonance energy in conjugation. It seems likely that analogous ionic structures are important in all forms of conjugation and of hyperconjugation, both sacrificial and isovalent.)

Conjugation in diacetylene, according to π -electron theory, is entirely analogous to that in butadiene, except that it is *two-dimensional* instead of one-dimensional: predominant structure HC $\#C$ -C $\#CH$, secondary structures HC $\#C$ $\#C$ $\#CH$, $HC_0^{\pm}C\overline{+}C^{\pm}CH$, and (very minor) $H\zeta-C\overline{\div}C-\zeta H$.

Examples of a structural situation which on the basis of quantum theory should also be described as conjugation occur in the cumulcncs. for example one-dimensional conjugation for $H_2C\text{=C}\text{=C}\text{=CH}_2$ with secondary structures $H_2\text{C}-C\text{=C}\text{H}_2$ and two-dimensional conjugation for $H_2C\text{+C}\text{+C}\text{+C}$, with secondary structures $H_2C-C \neq C-C \neq CH_2$ and $H_2C = C \neq C-CH_1$.

Ordinary first-order hyperconjugation is similar to ordinary conjugation in that there is one principal VB structure, and one bond is lost in the subordinate structures. It differs, however, in that the lost bond is a $[\pi]$ instead of a π bond. For example, in propylene (one-dimensional hyperconjugation) with main structure $H\rightleftharpoons C-CH^{\pm}CH_{2}$. the subordinate structures are H_3 ² \rightleftarrows C \pm CH₂. In methylacetylene (two-dimensional hyperconjugation) with main structure $H₃\equiv C-C\neq CH$, the major subordinate structures are $H_3^{\circ} \rightleftarrows C \rightleftarrows C \rightleftarrows H$ and $H_3 \rightleftarrows C \rightleftarrows C \rightleftleftarrows C$. Another example of twodimensional hyperconjugation is found in allene, with main structure $H_2 \# C \# C \#$ $C=\mathbf{H}_1$ and secondary structures H_2 -C $\neq C$ - $\stackrel{\rightarrow}{C}$ -H₂ and $H_2 \neq C$ -C $\neq C$ - H_2 . Here the term hyperconjugation is used to describe *3* situation analogous to conjugation in the cumulenes.

First-order hyperconjugation, like conjugation in butadiene and diacctylene, involves *two-way* dative action in the ionic subordinate VB structures. However, this may be slightly polar, in the sense that, for example in propylene, the structures H₃ $\pm C\pm CH-C$. H₂ may be a little more prominent than H₃ $\pm C\pm CH-C$. H₂, leading fo a slight over-all polarity and dipole moment. But there is no theoretical justification for assuming that only the former of these two structures is important. In fact it is by no means clear theoretically that *either* of the two ionic structures should be comparable in importance with the long-bond structure $H_{3\pm C}^{\dagger}C \pm CH-CH_{2}$. It seems

¹⁹ R. S. Berry, *J. Chem. Phys.* (1959); based on wave functions obtained by him previously [*J. Chem. Phys.* 26. 1060, (1957)]. For certain rather esoteric qualifications on the meaning of the percentages quoted, reference must be made to his new article.

²⁰ W. T. Simpson, J. Amer. Chem. Soc. 73, 5363 (1951); *Ibid.* **77, 6164 (1955).**

H+ to the writer that the customary use of a symbolism such as $H - C = CH - C$ \mathbf{H}^{\prime}

and corresponding emphasis on electron release, without any mention of an oppositely polarized ionic structure and, espaoially, of the long-bond structure, may be seriously misleading.

[*Note added* 20 *November* 1958. Berry's calculations on butadiene lend strong support, by analogy, to these remarks. At the same time the probable importance of dispersion-type ionic structures offers a rcaronable mechanism for appreciable electron release, through mild predominance of H_3 + \rightleftharpoons C --C·H-C-H₂ over $H_3 = C^+ - C^-H - C^+H_2.$

In this connection, the fact, emphasized by Dewar, that the observed dipole moments in propylene and other hyperconjugated molecules can be explained without H'

assuming such structures as $H_{\text{C}}C$ CH-CH₂ to be of appreciable importance, is H'

significant. It seems then entirely possible that *both* the above-indicated ionic structures arc of minor importance in typical cases of ordinary hyperconjugation. This, however. would not necessarily imply that the *long-bond* structure is also unimportant, nor that ionic structures are *always* unimportant in hyperconjugation. [Note *added 20 November* 1958. It seems likely that n-electron resonance may contribute appreciably to the dipole moment through a mild preponderance of H_5 ⁻ = C⁻-C⁺ -C⁻ over $H_3^- = C^+ - C^-$. (The structures H_3 . C-C=C and $H_3^- - C^-$ -C .= C with the former preponderant need not be considered here, since they would also be present in the CH₃ group in the absence of π -electron hyperconjugation resonance.)

Bcforc going further, an important difference between isovalent and sacrificial conjugation and hyperconjugation should be emphasized: while in the isovalent cases three important subclasses (dative, non-dative. and homodative) need 10 be distinguished, in the sacrificial case most examples (Including all those thus far discussed) belong to the non-dative (or two-way dative) subclass. However. there is also a dative sacrificial subclass, whose most familiar examples are the nitro-compounds, for ex-

ample nitrobenzene (four isovalent main structures such as $\bigotimes_{i=1}^{\infty} N$ with four

 π_x bonds, and three sacrificial one-way dative structures such as $\leftarrow \rightarrow \infty$. Nitroethylene, nitroacetylene, and the like, would belong to the same subclass. Similarly, nitromethane is an example of dative sacrificial hyperconjugation (main \mathcal{L} structure $H_3 \equiv C-N$, sacrificial one-way dative structure $H_3 = C-N$ O. the other hand, p-nitroaniline. like aniline, is an example of dative isovalent *conjuga*tion (main structures such as $H_sN-\ll \searrow N$), isovalent dative structure $H_{\mathbf{r}}N=\langle I_{\mathbf{r}}\rangle=N\langle I_{\mathbf{r}}\rangle.$

in stabilizing respectively the ally1 and methyl derivatives of aldehydes and ketones.

In fulvene, the presence of polar conjugation to an extent sufficient to create a dipole moment of about I.2 D, and in the theoretically expected direction, seems to have been definitely established.²¹ Besides the predominant VB structure \rightarrow CH₂. *Y,* there should here be five sacrificial structures, for example \geq \leq \le five corresponding structures with the charges reversed, and four long-bond structures such as **Fig. Set Executed 20 November 1958.** Again, dispersion-type ionic **properties** structures, for example, $\overrightarrow{CH_2}$, are doubtless important.]

This case differs in an important way from that of butadiene or acrylaldehyde in which there is only one structure of each type $(- + + + -$, and $\cdot \cdot$). Namely, isovalent **resonance** (homodative. moreover, in the cases of the ionic structures) can occur within each group of sacrificial structures, causing pronounced extra stabilization. Under these circumstances, one may reasonably expect conjugation to have much more important effects than in butadiene or acryIaldehyde. But further, in view of the special, benzene-like, stability of the *cyclopentadienyl anion*, it is reasonable to expect the ring-negative structures to predominate over the others. This result is confirmed theoretically by LCAO-MO computations and experimentally by the observed dipole moment.*I

Similar results and conclusions have been found²¹ for azulene. Here there is a large *number* of sacrificial conjugated structures, resonance among which should make conjugation important here. Further, the known benzene-like stability of the cyclopentadienyl anion and the tropylium cation lead one to expect an over-all negative charge on the five-ring and positive charge on the seven-ring, and a dipole moment of corresponding polarity. The observed dipole moment is 1.0 D, which (although its sign has not been dcmonstratcd experimentally) seems to be in reasonable agreement with the results of LCAO-MO computations.²¹

 $cyclo$ Pentadiene is the hyperconjugative analogue of fulvene, with a main structure $\overline{}$ $\| \cdot \|$ $\frac{1}{\sqrt{2}}$ is the same regative members may be expected to predominate for the same reason \mathbf{H}_2 and five sets of sacrificially hyperconjugated VB structuressuch as \mathbf{H}_2^* . as in fulvene. $²²$ </sup>

IV. HYPERCONJUGATION IN POSITIVE MOLECULE-IONS

Particularly in mass spectroscopy, there is increasing interest in the structure of positive ions. In even-electron ions (radical ions), homodative isovalent conjugation or hyperconjugation appears to have an important stabilizing effect [cf. Sections II(b) and II(d)]. In odd-electron ions (molecule ions) we encounter also homodative situations which arc half-way between isovalcnt and sacrificial. Observed ionization

²¹ G. W. Wheland and D. E. Mann, J. Chem. Phys. 17, 264 (1949). The measurements were actually made on several derivatives, rather than on fulvene itself, but the reasoning back to fulvene seems convincing. Azulene: see **Bernstein and J. A. Pople, J. Amer. Chem. Soc. 80, 3497 (1958).**

n For results of **l.CAO-MO** calculations, cf. G. Berthier and B. Pullman, *Bull. Soc. Chim. Fr.* 15. 788 (1948); B. Pullman and A. Pullman. Les Theories Electroniques de la Chimie Organique. **Masson et Cic, Paris (IY52).**

In non-dative sacrificial conjugation and hyperconjugation, one may of course distinguish between non-polar and polar cases (i.e., symmetrical or unsymmetrical two-way dative action), but the distinction is one of degree rather than kind. For example, conjugation in butadiene is necessarily non-polar, by symmetry, whiie firsforder hyperconjugation in propylene must be polar, though perhaps only slightly so.

At this point something should be said about ordinary *second-order hyperconjugalion.* This is now believed⁶ to be a very small effect, and because of its universality **It is difficult or impossible to isolate experimentally, but there Seems to be no adequate reason to dismiss it as entirely negligible. Typical examples arc found in ethylene** (principal VB structure $H_1 \rightleftarrows C \rightleftarrows H_2$, hyperconjugative structures $H_2 - C \rightleftarrows C - H_2$) and ethane (principal structure H₃宗C-C壽H₃, main hyperconjugative structures H₃^{\pm}C \pm C \pm H₃ and H₃ \pm C \pm C \pm H₃). It will be noticed that second-order hyper**conjugation is one-dimensional in ethylene. two-dimensional in ethanc; also that is non-polar in both cases.**

Characteristic of second-order hyperconjugation as described by VB structures is the fact that *two* $[n]$ bonds are sacrificed, while one π bond is gained. There is, however, a net loss of one (π or $[\pi]$) bond just as in ordinary conjugation or first-order **hyperconjugation; but it should be noted that this occurs in a way which differs from hyperconjugation in the same way that hyperconjugation differs from conjugation, so** that the effect might well be called *hyper-hyperconjugation*.

Antxample in which the LCAO-MO treatment of second-order hypcrconjugation differsconsiderably from the usual VB treatment is found in the ethyl ion.' Here (in addition to isovalent hypcrconjugation) we have second-order hyperconjugation involving in the VB method just the main structure $H_a \neq C-C$ ⁺ \overrightarrow{H}_a and the subordinate structures $H_s \rightharpoonup C \rightharpoonup H_s$. The LCAO-MO treatment¹ (provided suitable electro**ncgativitydi!Terencc parameters are introduced) automatically includes also an** important amount of the structure $H_3 \equiv C - \bar{C} - \bar{H}_2$ in which the right-hand carbon atom as a whole is neutral. From the VB standpoint, the inclusion of this structure would be **called an inductive eficct. This is a rather extreme example of a characteristic feature of the LCAO-MO method which automatically includes any inductive effects which** may occur in the π -electron system (σ -electron inductive effects--cf. Section II(a)-**are of course not included).**

(b) *Polar egPcrs in conjugation and hyperconjugarion*

As has been emphasized in Section III(a), the ionic secondary structures in ordinary "non-dative" conjugation and hypcrconjugation occur in pairs of opposite polarity. The result may be non-polar, but if the atoms or groups bctwccn which, in these ionic structures, charge transfer takes place, differ in electronegativity, then some net polarity results. For conjugation, a simple example is H₂C⁻ CH-CH- O, in which **the secondary structure H,C.-CH -CH-O obviously would predominate over H,C -CH .- CH-0** **. [Note added 20 Nor.emher 1958.* **Probably much more important** is predominance of H₂C⁺-C H-C⁺H-O⁻ over H₂C⁺-C⁺H-C⁻H-O⁺.]² For hyperconjugation, a similar example is $H_3 \equiv C - CH_1 \cdot O$, where H_3 : $C - CH - O$ must pre**dominate over Ha C CH-0..** *[Nore added 20 Nowmher* **1958. Probably much** more important is predominance of H_3 \div C \div C \div H \div O⁻ over H_3 ⁻ \div C \div C \div H \div O \div .] It seems possible that the polar effects in these cases may be of appreciable importance potentials suggest that these ions also are rather strongly stabilrzed by conjugation and hyperconjugation.

The C_2H_4 ⁺ ion has already been discussed in Section III(e). For planar C_2H_4 ⁺, isovalent resonance between the two main structures H_2C ⁻-CH₂ and H_2C -CH₂. each a single-bonded structure, results in the equivalent of a half π bond. This may be summarized as $H_2C' = C'H_2$, where C' means C^{-1} .

The ionization potential of 1,3-butadiene is 1.45 V smaller than that of ethylene. This fact can be understood²³ in terms of much greater π_{x} -electron resonance stabilization by conjugation in the positive ion than in the neutral molecule. In the positive ion, the main VB structures may be described as $H₅C = CH-C'H = C'H$, and $H_2C' = C'H - CH$ CH₂ (that is, $H_2C = CH - C'H - CH_2$, $H_2C = CH - CH - C'H$, with resonance, and $H₁C$:-CH-CH :--CH₂, H₂C-C H -CH ==CH₂ with resonance). Isovalcnt resonance between these is supplemented by resonance with the half-sacrificial structures $H_2\dot{C}-CH = CH - C⁺ H_2$ and H_2C -CH =CH-CH₂, the over-all result being a much stronger conjugative effect than in the butadiene molecule. [Note added 20 *November* 1958. Probably dispersion-type structures such as H₂C $-C$ H-C $H-C$ ⁺H-CH₂ are also important.]

Homodative resonance within the π_{z} -electron system here distributes the positive charge fairly evenly over the carbon atoms, but a small amount of σ charge redistribution, by inductive effects in the σ bonds, must occur to alleviate in part an excess π , positive charge on the two outer carbon atoms. Some further redistribution of charge by inductive electron release from the hydrogen atoms, via the C-H bonds, must of course also occur, and thereby contribute somewhat to the stabilization energy. But it seems likely that the major part of the stabilization energy is due to π_x -electron resonance.

In the positive ion of propylene, C_3H_6 ⁺, with main structure $H_3 \oplus C-C'H^{\perp}C'H_2$ one has homodative isovalent half-hyperconjugation with $H'_3 \rightleftharpoons C'-CH \rightleftharpoons CH_2$ and homodative half-sacrificial hyperconjugation with H_3 \div C \pm CH-CH₂ and H $\frac{1}{3}\div$ C \pm CH-C·H₂ (altogether two main and four subordinate **VB** structures). The minimum ionization potential of propylene is 0.79 V lower than that of ethylene.²⁴ The difference may reasonably be ascribed largely to stabilization of the positive ion in consequence of methylation. (There is no reasonable doubt that it is a π _z electron which has been removed in the ground states of both the ethylene and the propylene ion.) Further, the stabilization energy can reasonably be identified in considerable part with homodative hyperconjugation energy, the situation being similar to that in the ethyl **ion** and in the toluenium ion [cf. Section Ill(d)]. However, electron release from the several hydrogen atoms by non- π_x (i.e. σ , [σ], and [π_y]) inductive effects must contribute very considerably to the stabilization energy (as also, though to a lesser extent, in the alkyl and methylatcd-benzene carbonium ions).

Observed further lowerings of ionization potential by further mcthylation or alkylation of ethylene²⁴ may be accounted for in the same way. A similar explanation can be given for the fact²⁴ that alkylation considerably lowers the ionization potentials of unsaturated and aromatic hydrocarbons m general.

²³ J. Fain and A. L. Matsen, J. Chem. Phys. 26, 376 (1957).
²⁴ W. C. Price, Chem. Rev. 41, 257 (1947) lists the ionization potentials of a large number of com-
pounds and their alkyl deratives (but see K. Watanabe, J. better values of some of the ionization potentials). He explains the lowering of ionization potentials by methylation in much the same way as here.

The alkyl derivatives of HCl, H_2O , H_3S , NH_a and like molecules constitute another class of molecules in which substitution of alkyl groups for hydrogen atoms gives rise to lowered ionization potentials.²⁴ Here again, as in the alkylated aromatic and unsaturated compounds, hypcrconjugation should help to stabilize the molecule ions. However, it is of a different and probably weaker type than in the unsaturated systems.

As examples, let us consider $CH₃OH$ and $CH₃Cl₂$. In the ground electronic state of ionized CH₂OH, the main VB resonance structure is $H_3 \equiv 1C \rightarrow \tilde{O}H$. The most important subordinate structures are $H_s^{\bullet} \rightarrow C \rightarrow O^+H$ (involving isovalent hyperconjugation without charge transfer, i.e. non-dative) and $H'_3 \equiv C'$ -OH (involving homodative half-sacrificial half-hyperconjugation: i.e. half of one $[n_x]$ bond is lost, but homodative transfer of positive charge from the O atom to the CH_a group is accomplished). For CH₃Cl⁺, the ground electronic state must be two-fold degenerate (${}^{4}E$ state), corresponding to removal of either a π_x or a π_y chlorine electron. The two substates are equivalent but independent; let us then consider just the one with a π_x electron removed. This is completely similar to CH₃OH⁺: the main structure is H $\frac{1}{\sqrt{2}}C \cdot \frac{C_1}{C_2}$ and the chief subordinate structures are $H_x=SC=Cl^+$ and $H'_x=Cl^--Cl$.

It will be noted that *homodative isoralent* hyperconjugation, the strongest type of hypcrconjugation, present in the ions of propylene and other alkylated aromatic or unsaturated compounds, is no longer present in CH_3OH^+ , CH_3Cl^+ , and the like. Hence it is reasonable to expect that non- π inductive effects may be more largely responsible for charge equalization and resulting stabilization in the latter than in the former. For the alkyl halides RCI, RBr, and RI, there is indeed strong spectroscopic evidence²⁵ indicating that hyperconjugation makes only relatively minor contributions to the structure of their positive ions; in other words, that the actual structure is not far from being $H_3 \equiv C \sim C l^+$ alone.²⁴ However, it is generally believed that π bonding is weaker in higher-row than in first-row atoms, so that the conclusions derived from the spectroscopic evidence just cited may not apply with full force to. $(CH_3F)^+$ and the ions of alkyl derivatives of H_2O and NH_3 .

V. PLUVALENT CONJUGATION

Besides sacrificial and isovalent conjugation. there are a few cases in which conjugation occurs which may be described as *plucalenr* (one *more* bond in the sccondar) than **in** the **main VB** structure). Only *dotice* pluvalent conjugation is to be expected.

An example is BF₃ with main structure F_{+B} \langle and three equivalent pluvalent struc λ E

turcs of the type F-R $\mathcal{L}^{\mathbf{r}}$ As is well known, resonance here causes strong stabiliz
 \searrow_F tion. \mathbf{F}

²⁴ R. S. Mulliken, *Phys. Rev.* 61, 277 (1942): see especially footnote 9 and Table II, second column. **24** This would be in accord with views earlier expressed by the writer, in which (a), the relatively low ionization potentials for example of H_2O as compared with O and of HCl as compared with Cl, and (b), the still l **ken** *J. Chem. Phys. 3, 514 (1935)—but see K. Watanabe <i>J. Chem. Phys. 26, 542.* **1773** (1957) for more reliable ionization potentials (which give a more consistent picture than the earlier **values).]**

Another example in which pluvalcnt conjugation may be of non-negligible importance is HF with main structure H--F and pluvalent conjugated structure H \exists **F.** Similar structures may be of appreciable importance in hydrides in general,²⁵ at **least where the H atom has bccomc distinctly positive. enabling it to some extent to** hold an electron in the excited H⁻ state 1s $2p\pi$.

VI. THE RELATIONS BETWEEN INDUCTIVE AND MESOMERIC EFFECTS

Inductive effects, and their interaction with mesomeric effects, have been referred to several times in the preceding Sections. Since the two effects cannot always be sharply separated. especially in hyperconjugation. and since confusion (more of language than of understanding) can and does arise, it seems desirable to survey the relations between them.

To begin with, it may be worth while to remind the reader that ordinary inductive **effects correspond, m VB theory. to resonance between covalent and ionic structures. It** will simplify **the discussion if at first we ignore hypcrconjugation with its quasi-a** and quasi- π bonds, and think only in terms of σ and π bonds (including both π_x and π_{ν} in the case of triple bonds) in the usual sense. Both σ and π bonds can be polar, that is, can exhibit the inductive effect. From what is known of the polarizabilities of σ and π electrons, one expects the π bonds to be more strongly polar than the σ bonds, **but both polarized in the same direction, in unconjugated polar double or triple**

bonds (example $\begin{array}{c} H \\ H \end{array}$): Polarity is expected when the atoms connected by a

multiple bond belong to different elements, or when. if they both belong to the same element, they differ in charge or (in the case of σ bonds) in degree of $s-p$ hybridization. **In conjugated systems,** *procided* **the conjugation is not dative or homodative, the** inductive or polarity effect is not essentially different quantum-mechanically than in unconjugated systems such as for example, $H_1C \rightrightarrows CH \rightarrow C \rightrightarrows O$.

In dative and homodativc isovalcnt conjugation, however, there is either a strong cooperative, or a strong joint, inductive-mesomeric effect [here see also Section II(a)]. In dative conjugation the dative charge shift in one direction in the π -electron system **should be accompanied typically by an** *oppositely* **directed "inductive" shift in the** σ bonds; through this cooperative action, a *larger* "mesomeric" π -electron charge

/"F shift should occur than would be possible without it. [Example: H_2C_2 **2, with**

fF' subordinate structure H₃C → C_K and Here, in terms of quantum-mechanical theory,
H

F.-

'\H

the arrowheads are shorthand for a variety of ionic structures of which H,C- C *

is the most important. In total, the F atom gives a fraction of a π_x electron (dative conjugation), but receives a rather different, probably larger fraction of a σ electron **(inductive effect),]**

In homodative isoconjugation, the mcsomcric effect already.inrrinsically involves

a considerable amount of π_x electron shifting, in such a way as to partially but by no **means entirely even out the** π_x **charge distribution as compared with that in a single** one of the isovalent structures. One may reasonably describe the result as a joint **mesomeric-inductive effect.** *Further* **charge equalization can then take place by the** ordinary inductive effect in the π and especially in the σ bonds. The polarity re**adjustments in the** σ **bonds may here be described as** *cooperative* **in the same sense as in dative conjugation, and just as in that case should make possible larger mcsomcric effects than would occur otherwise.**

In summary, both mesomeric and π -electron inductive effects are resonance effects **according to VB theory. In ordmary semi-empirical LCAO-MO theory, both reson**ance parameters β and *inductive* parameters δ (and ω , if there are charged atoms¹)—or **the equivalent of these if the self-consistent-field method is used (cithcr in its original** form or in the Pariser-Parr or the Pople modification) -arc introduced at the outset. **It is then in general scarcely feasible to say, except qualitatively, how much of the total computed effect is due to covalent resonance, how much to bond-polarities (inductive effect), and how much to a mutual interactjon of the two.**

furning now to hyperconjugation, we first replace some sets of σ **bonds by [** σ **]. [n,], and [n,] GO (group orbital) bonds [cf. Section I(b)]. This procedure represents** a partial adoption of the LCAO-MO viewpoint, after which, however, we can then **carry the discussion further using the VB method. This last has been done in the** present classification of hyperconjugation into types and subtypes. The $[\pi_x]$ bonds are now treated in the same way as π_x bonds, and all that was said above about the **inductive and mesomeric effects in conjugation bccomcs directly applicable also to hyperconjugation.**

In all cases where the hyperconjugation is intrinsically *two-dimensional*, $[\pi_{\mathbf{v}}]$ and $[\pi_x]$ hyperconjugation must be treated alike, and what has been said about $[\pi_x]$ hyperconjugation then applies equally to the $[\pi_{\nu}]$ bonds. But otherwise, it is a matter of choice as to whether one wishes to consider $[\pi_{v}]$ hyperconjugation. In particular, second-order hyperconjugation is a form of $[\pi_{\nu}]$ hyperconjugtaion which for many **purposes can be ignored, since it must usually bc a rclativcly small effect and slncc. because of its universal background prcscncc, it probably does not lead to appreciable observable differences in molecular propcrtics [cf. last paragraphs of Section Ill(a)].**

However, the I CAO-MO 'treatment of second-order hyperconjugation, because it includes an inductive parameter, yields a considerable stabilization energy in cases where transfer of a π_y electron can reduce charge inequalities, as for example in the **ethyl ion.' From the VB standpoint, however. this LCAO-computcd stabilization** energy is nearly all due to an inductive effect in the $\pi_{\mathbf{y}}-[n_{\mathbf{y}}]$ electron system [cf. last **paragraph of Section Ill(a)].**

As already noted, $C = R_3$ and $C = R_2 \sigma$ bonds are treated in hyperconjugation in part like π_x bonds and in part like π_y bonds (and in part like σ bonds). In one-dimensional hyperconjugation (π_x and $[\pi_x]$ only), what would be classed as inductive effects **if hyperconjugation w'cre ignored arc now classed** *k purr* **as mcsomeric (or as mixed inductive-mesomcric) effects. In two-dimensional hyperconjugation. a similar statement applies in double mcasurc. Thus in speaking of inductive and mcsomeric effects in hyperconjugated systems. it is desirable to take special care as to just what is meant by these terms. Perhaps It would be better If less emphasis than is customary were** placed on trying to distinguish and separate them.

VII. HYPERCONJUGATION AND THE BAKER-NATHAN EFFECT

Baker and Nathan,?' in first introducing the ideas which Baker identifies with hyperconjugation. 2" suggested that when a "methyl group is attached to a conjugated system, the duplet of electrons forming the C-H bond in this group are appreciably **less 'localized' than arc those in a similarly placed C-C bond," and referred to the effect as a "new mechanism of electron release" " which either cannot function or is grca'ly dimmishcd in the higher alkyl groups." In later papers it was assumed to decrease from a maximum for Me to zero for I-Bu. They used it initially to explain data on the velocity of interaction, by a bimolecular (Ss2) mechanism, of various alkyl-substituted benzyl bromides with pyridine in dry acetone, where for a single p-alkyl substituent they found that the velocity decreased by small amounts in the order Me** $> Et > i$ **-Pr** $> t$ **-Bu** $> H$ **. They then extended the application of the idea in various directions.**

In their preceding paper,²⁹ they indicated a belief that the activated state in the **bimolecular reaction with pyridine is one which involves incipient anionization of the bromine atom, and is therefore speeded by easier electron release from the p-alkyl (or other) substitucnt group (or groups) in the substituted benzyl bromide.** *Complete* **anionization of the bromine would create a benzyl carbonium ion in which p-alkyl** substitution should give rise to homodative isovalent hyperconjugation (main structures $H_3 = C \left(\begin{array}{c} \sim \\ \sim \end{array} \right) - \dot{C}H_2$ and three ring-positive structures; hyperconjugated structure H_a = $C \quad \left\langle \quad \right\rangle = CH_a$) closely similar to that in McCaulay's methylated-

benzene carbonium ions [cf. Section II(d)).

The concept of hyperconjugation as defined by the present writer³⁰ referred to **definite states of individual molecules, mainly ground states but also spectroscopically excited states; it was also obviously applicable to radicals and ions. In some of his** later papers,³¹ Baker adduced evidence that the Baker-Nathan order (Me $> Et$ $>$ $i\text{-}Pr > t\text{-}Bu > H$) holds for the ground as well as activated states of certain hyper**conjugated 'systems. He concluded that, for example in p-alkyl benzaldehydes, in -**

addition to stabilization of the main VB structure R,Cy \-CH-O by struct-\= ./ ures $R_3C-\ll$ \geq \geq \sim CH \cdot O. (inductive effect, or polar character, of the C $=$ O π bond) **CH-0' (ordinary or sacrificial conjugation in the present term-** , by R₃C⁺-C $\langle \rangle$ -CH: O (inductive effect or polar

- ²⁷ J. W. Baker and W. S. Nuthan, *J. Chem. Soc.* 1844 (1935).
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²⁸ J. W. Baker, *Hyperconjugation*. Oxford University Press (1952).
²⁹ J. W. Baker and W. S. Nathan, J. Chem. Soc. 1840 (1935).
³⁰ R. S. Mulliken, J. Chem. Phys. 7, 339 (1939); cf. reference 3 in this paper with rega cluded "that hyperconjugation changes (most likely decreases) the energy of the normal state"
but that "the change is probably considerably smaller than for the [spectroscopically] excited
states". ³⁰⁸ Regarding some pre J. Amer. Chem. Soc. 63, 41 (1941). Regrettably, the papers of Baker and Nathan, and of Baker and
other collaborators had not then come to our attention. ³⁰ A still earlier example, of what would here be called isovalent hyperconjugation, is contained in the writer's discussion of the theory of **~hc struclurc of iwisrcd elbylenc in** *f'hrs. Rrr.* **43. 27Y (1933).**

I1 J. W. Baker. 1. *('hon. Sac-. 191 (IY42); /hid. US* **(1938); 7Y6 (IYJI): t/.,,prrronjullorion. Oxford** University Press (1952).

character in the σ bond from R₃C to the ring), and finally by R₃⁻C $=$ **_.. / CH-0** -

(ordinary or sacrificial hypcrconjugation in the prcscnl terminology) but with a maximum effect of this last structure for $R = H$ **and no effect for** $R = CH_3$ **.**

In two respects the quantum-mechanical theory of π -electron resonance in hyper**conjugation seems to deviate strongly from the ideas prrscnted by Baker.**

(1) The theory gives no indication that the hyperconjugative π -electron resonance

power of a group \mathbb{R}' - \subset should depend in an essential way on how many of R, R'. **R"/**

and R" are H atoms. Qualitatively, bonds from H atoms. Me or other alkyl groups or indeed from any atom or group should be alike capable of participating in hypcrconjugative resonance. Quantitative differences would be expected, of course; a C-C bond from Me might be less (or more) effective than a C-H bond from H,³² but **it would not bc cxpectcd lo bc negligibly effective. nor is thcrc any obvious reason why it should be radically different in cffectivencss. This statement applies both to ordinary and IO isoialcnt hypcrconjugation.**

In any event. the Bakel-Nathan cficct. m so far as it pertains to diffcrcnccs bctwcen C-H and C-C hypelconjugation. should not itself bc called hypcrconjugation, although it might be called *differential* hyperconjugation (for C -C relative to C -H).

Taft's Confcrcnce paper includes a thorough discussion of evidence of various kinds that π -electron resonance occurs for C-C as well as for C-H hyperconjugation although (in accord with the Baker-Nathan effect) more strongly for the latter. The **c\ idencc pertains both to ground state. hypcrconjugation and to activated state hypcrconjugation (reaction rates. etc.).**

(2) The theory [set detailed discussion of butadiene and propylene in Scction Ill(a)] dots not indicate that ordinary hyperconjugation should in general be an important ekctron-release mechanism (nor that, if it were, H should be better than Me-rather the contrary).

[.Vore a&i4 20 A'ocvmber 1958. The probable importance of dispersion-lypc ionic states now furnishes a reasonable theoretical basis for appreciable electron rclease in hyperconjugation; and perhaps also for greater release in C-H than in C-C hyperconjugation, since H is more electropositive than C, and therefore $H_3 \equiv$ or

 $\,H_2$ = than e.g. (\rightarrow C)₂ = or (\rightarrow C)₂ = .] *Maximum strength* of hyperconjugative effects,

including electron release, should occur in homodative isovalcnt hyperconjugation, as for example in McCaulay's alkylated aromatic carbonium ions [cf. Section II(d)].

In so far as the Baker-Nathan effect is concerned with activated states in chemical reactions, it is more difficult 10 say what might be expected theoretically than when one is concerned only with molecules or ions in ground (or definite spectroscopically excited) states. Presumably activated states are more affected by steric factors than ground states. Solvent effects can of course be important for any state. particularly for an ionic or highly polar state. However, when activated states involve incipient

^{&#}x27;* R. S. Mulliktn and R. G. Parr. J. Chrm. *Phvs. 19. 1271 (1951).* **Equalton (23a) and footnote** *26* **of** this paper attributed variations in heats of formation of variously branched hydrocarbons to Rreater C-C than C-H second-order hyperconjugation energies. However, especially in view of the theoretically expected smallness of all second-order hyperconjugation effects,⁵ their attribution must be considered speculative.

carbonium ion formation, they should presumably involve incipient homodative isovalent hyperconjugation. Taft's Conference paper indicates that the relative importance of C-H and C-C hyperconjugation is similar in activated and ground states.

In connection with the role of hyperconjugation in reaction mechanisms, a survey by Wheland³³ of the explanation of the Markovnikov rule for the addition of reagents of type HX lo a double bond is of interest. It is assumed that the reaction proceeds through a (perhaps only incipient) carbonium-ion-salt activated complex. The explanation is then essentially that, taking propylene as the simplest example, the isopropyl ion, with main structure $H_3 \triangleq C$ -CH-C $\triangleq H_2$, is stabilized by two (homodative isovalent) hyperconjugated structures $(H₃ \pm C-CH \pm C$ - H * and $H^+ = C \pm CH - C \equiv H_3$, whereas the propyl ion $H_3 \equiv C - C - C^+ = H_3$ is stabilized only It H,

by one $(H_s\equiv C-C\equiv H_s)$. Hence the *iso*propyl-type complex is more stable and Н.

the addition takes place accordingly. Mass spectroscopy as well as hyperconjugation theory furnishes evidence for the greater stability of the isopropyl than of the propyl ion; however. there arc also questions of the geometry of the actual ions, but it would lead too far to attempt to discuss these questions further here.

³³ G. W. Wheland, *Resonance in Organic Chemistry*, pp. 430 *et seq.* Wiley, New York (1955);
C. K. Ingold, *Structure and Mechanism in Organic Chemistry.* Cornell University Press, Ithaca